



# Simplified model for hydrogenotrophic denitrification in an unsaturated-flow pressurized reactor

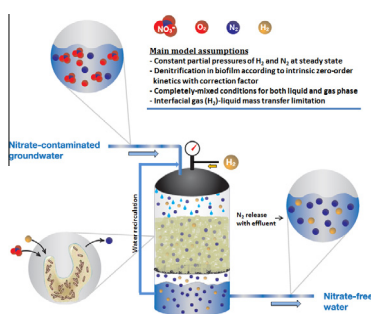
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## HIGHLIGHTS

- A model for H<sub>2</sub>-based denitrifier unsaturated-flow pressurized reactor is presented.
- The rate constant and  $k_La$  were determined for different recirculation flow rates.
- A correction factor for the rate constant was successfully developed.
- High correlation between model and experimental results was achieved.
- Max. denitrification rate of 7.5 gNO<sub>3</sub><sup>-</sup>-N/(L<sub>reactor</sub>·d) was predicted by the model.

## GRAPHICAL ABSTRACT



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## ABSTRACT

A novel unsaturated-flow pressurized reactor (UFPR) for hydrogenotrophic denitrification was recently developed. The reactor is characterized by safe and economic operation since gas purging intrinsic to conventional H<sub>2</sub>-based systems is not required and H<sub>2</sub> loss is limited only to the dissolved H<sub>2</sub> in the effluent. Additionally, high denitrification rates are achieved by high water recirculation over plastic carriers with high surface area.

This paper focuses on mathematical modeling of the novel reactor, based on its unique and specific characteristics. The continuously stirred hydraulic regime formed due to the relatively high recirculation flow rate required for efficient media wetting and the homogeneous gas phase in the closed reactor head-space, simplified the model design for the UFPR. The reaction rate constant and the overall volumetric gas (H<sub>2</sub>)-liquid mass transfer coefficient ( $k_La$ ) were determined for different recirculation flow rates at steady state. A rate constant correction factor  $\beta$  was developed to compensate for pH changes within the biofilm, deviation from intrinsic zero-order degradation kinetics and non-homogeneity of the biofilm. Model validation tests showed a high correlation between experimental and model results for various combinations of operational parameters. Results from the model showed that high denitrification rates of up to 7.5 g NO<sub>3</sub><sup>-</sup>-N/(L<sub>reactor</sub>·d) together with H<sub>2</sub> utilization efficiencies above 90% can be achieved by the UFPR.

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## 1. Introduction

Hydrogen-based denitrification systems for treating nitrate-contaminated groundwater have gained a lot of attention in recent

years. The clear advantages of hydrogenotrophic systems over reactors using traditional organic compounds as electron donors for reducing NO<sub>3</sub><sup>-</sup> have been extensively discussed in previous works and include mainly low biomass yield, minimization of reactor clogging and reduction of post-treatment costs. However, safety concerns, poor utilization of H<sub>2</sub> gas and low denitrification rates are the main drawbacks still limiting the implementation of this method in full scale [1].

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## Nomenclature

$A$	total active surface area for bacterial growth [ $\text{m}^2/\text{m}^3$ ]	$N_e$	effluent concentration of $\text{NO}_3^-$ -N [mg/L]
$\beta_H$	empirical correction factor for $K_H$	$N_i$	inlet concentration of $\text{NO}_3^-$ -N [mg/L]
$\beta_N$	empirical correction factor for $K_N$	$N_{2,T}$	total dissolved $\text{N}_2$ concentration [mg/L]
$C_{H_2}$	Henry's constant for $\text{H}_2$ gas [mg/(L·bar)]	$N_{2,atm}$	dissolved $\text{N}_2$ concentration originated from atmospheric $\text{N}_2$ gas [mg/L]
$C_{N_2}$	Henry's constant for $\text{N}_2$ gas [mg/(L·bar)]	$N_{2,denit}$	dissolved $\text{N}_2$ concentration originated from denitrification [mg/L]
$D_{f,H}$	diffusion coefficient of $\text{H}_2$ in the biofilm [ $\text{m}^2/\text{d}$ ]	$P_{H_2}$	partial pressure of $\text{H}_2$ gas in the reactor [bar]
$D_{f,N}$	diffusion coefficient of $\text{NO}_3^-$ in the biofilm [ $\text{m}^2/\text{d}$ ]	$P_{N_2}$	partial pressure of $\text{N}_2$ gas in the reactor [bar]
$H^*$	equilibrium concentration of dissolved $\text{H}_2$ [mg/L]	$P_T$	total pressure in the reactor [bar]
$H_{av}$	average concentration of dissolved $\text{H}_2$ along the filter [mg/L]	$q_{max,N}$	maximal specific degradation rate of $\text{NO}_3^-$ -N [g/(gVSS·d)]
$H_e$	effluent concentration of dissolved $\text{H}_2$ [mg/L]	$Q$	volumetric flow rate [mL/min]
$H_i$	inlet concentration of dissolved $\text{H}_2$ [mg/L]	$Q_R$	recirculation flow rate [mL/min]
$K_H$	half-order coefficient for $\text{H}_2$ degradation [(mg/L) $^{0.5}$ /d]	$r_H$	overall degradation rate of $\text{H}_2$ [g/(L $_{reactor}$ ·d)]
$K_N$	half-order coefficient for $\text{NO}_3^-$ -N degradation [(mg/L) $^{0.5}$ /d]	$r_N$	overall degradation rate of $\text{NO}_3^-$ -N [g/(L $_{reactor}$ ·d)]
$k_{of,H}$	degradation rate of $\text{H}_2$ in the biofilm [g/(L $_{biofilm}$ ·d)]	$t$	time component [d]
$k_{of,N}$	degradation rate of $\text{NO}_3^-$ -N in the biofilm [g/(L $_{biofilm}$ ·d)]	$V$	reactor volume [L]
$k_L a$	overall volumetric gas-liquid mass transfer coefficient of $\text{H}_2$ [1/d]	$\nu$	stoichiometric mass ratio [g $\text{H}_2$ /g $\text{NO}_3^-$ -N]
$N_{av}$	average concentration of $\text{NO}_3^-$ -N along the filter [mg/L]	$X_f$	biofilm density [gVSS/mL]

A novel unsaturated-flow pressurized reactor (UFPR) for hydrogenotrophic denitrification of groundwater operating at high denitrification rates together with minimal hydrogen loss and low risk was presented and described in an earlier publication [2]. The main novelty of this reactor is the operation under a pressurized closed headspace without any gas discharge. The common concern of  $\text{N}_2$  gas build-up in a pressurized denitrifying system is addressed by the idea that in continuous operation a gas-liquid equilibrium is achieved according to Henry's law and the effluent water carries excess  $\text{N}_2$  gas out of the reactor. Since  $\text{N}_2$  reaches equilibrium and is not accumulated over time, there is no need for gas discharge and  $\text{H}_2$  loss to atmosphere is limited only to the dissolved  $\text{H}_2$  in the effluent. The operation under low-pressure headspace consisting uniquely of  $\text{H}_2$  and  $\text{N}_2$  gases prevents hazardous  $\text{H}_2$ – $\text{O}_2$  contact and minimizes the risk of explosion in case of failure.

On top of the inherent advantages of safety and economics, the UFPR was designed to ensure high denitrification rates in comparison to existing hydrogenotrophic systems. The reactor is operated under an unsaturated-flow regime as a trickling filter where water is recirculated over plastic biofilm carriers with high surface area. The high surface area of the plastic carriers serves as a platform for both bacterial growth and gas ( $\text{H}_2$ )-liquid mass transfer, thus enabling high denitrification rates. Utilization of plastic carriers with very high surface area in unsaturated-flow reactors is susceptible to reactor clogging and is more commonly implemented in autotrophic trickling filters with low cell yield as in nitrification or the UFPR. In these systems very often a relatively high recirculation flow rate is applied in order to achieve full media wetting [3]. The recirculation ratio ( $Q_R/Q$ ) applied in the UFPR varies between 3 and 18, which is about one order of magnitude higher than the recirculation ratio in traditional trickling filters [4]. This high recirculation ratio, together with the assumption of a well-mixed and homogeneous gas phase in the closed headspace, differentiates the UFPR from traditional trickling filters; especially in terms of reactor hydraulics.

Trickling filter models attempt to take into account various processes affecting the contaminant degradation such as gas flow, phase transfer, diffusion within the biofilm, biological growth and structural changes of the biofilm. Due to the problematic characterization of the unsaturated flow through the carriers and its poorly understood mechanics, most of the models and design

approaches of trickling filters are empirical and therefore case specific [4–6]. The main objective of the current study is to develop a simplified and easy-to-use model for basic design and performance forecast of the UFPR, based on its unique operational conditions of unsaturated flow with high recirculation flow rate and operation in a closed headspace. Special focus is given to the effect of recirculation flow rate on reactor performance.

## 2. Considerations and guidelines for model design

Based on model objectives, the following assumptions were taken for model design: (1) steady-state conditions exist for all phases (gas, liquid and biofilm); (2) the biofilm is planar, one dimensional and completely homogeneous with uniform density  $X_f$ ; (3) the diffusion layer near the biofilm surface is neglected, i.e., the substrate concentrations on the biofilm surface equals the bulk concentration; (4) mathematical models of hydrogenotrophic denitrification are generally described by zero-order kinetics when substrate concentrations are much higher than the half-saturation constants (i.e.  $S_{\text{NO}_3} \gg K_{\text{NO}_3}$  and  $S_{\text{H}_2} \gg K_{\text{H}_2}$ ) [7–9]. Therefore, a  $\text{NO}_3^-$ -N reduction based on zero-order kinetics in the biofilm is assumed. Importantly, application of a zero-order kinetic model in biofilm reactors should be considered more carefully due to the gradual decrease of substrate concentration with increasing depth of the biofilm, as was also discussed by Atkinson et al. [10]. Moreover, in the case of denitrification, the pH gradient formed within the biofilm might also affect the maximal specific degradation rate  $q_{max}$  along the biofilm. Accordingly, a correction factor is added to the standard zero-order-based reaction rate constant for degradation in the biofilm to take into account these factors as will be explained later; (5) due to the high diffusivity of  $\text{H}_2$  in the gas phase of the UFPR, the rate limiting step for  $\text{H}_2$  transfer is the interfacial gas-liquid transfer; (6) in the UFPR a high recirculation ratio is applied so that the entire trickling filter may be considered as a single CSBR (continuously stirred biofilm reactor) unit with a uniform concentration of  $\text{NO}_3^-$ -N throughout the reactor. This assumption can be applied also for the dissolved  $\text{H}_2$  concentration due to the following reason: since the reactor headspace is sealed (i.e. pressurized), no natural gas convection (i.e. air draft) occurs as in traditional trickling filters. Therefore, assuming good mixing of the gas phase by molecular diffusion, any gradient of

H<sub>2</sub> concentration in the gas phase along the filter can be neglected and the driving force for gas-liquid transfer (i.e. the term (C\*–C) in Eq. (5) below) should have approximately the same value at any position in the reactor. Nevertheless, a minor gradient of the bulk concentration (i.e. S<sup>b</sup> in Eq. (1) below) for both substrates is expected along the filter axis even at high recirculation ratios, i.e., the effluent concentration in the reactor's bottom S<sub>e</sub> is slightly different than the concentration in the top part of the reactor where recirculated water is mixed with the inlet flow. Therefore, an average bulk substrate concentration along the filter axis, different than the effluent concentration S<sub>e</sub>, is taken for model design.

Utilizing assumptions (1) through (4), the expression for penetration depth of the rate-limiting substrate to the biofilm can be described by Eq. (1) [11].

$$L_{pen} = \sqrt{2S^b D_f / k_{of}} \quad (1)$$

where L<sub>pen</sub> is the penetration depth of the rate-limiting substrate; S<sup>b</sup> is the bulk concentration of the rate-limiting substrate; D<sub>f</sub> is the diffusivity of the rate-limiting substrate in the biofilm and k<sub>of</sub> is the degradation rate of the rate-limiting substrate within the biofilm and expressed by Eq. (2).

$$k_{of} = q_{max} X_f \quad (2)$$

where q<sub>max</sub> is the maximal specific degradation rate of the rate limiting substrate and X<sub>f</sub> is the biofilm density.

In an ideal CSBR (see assumption (6) above), the penetration depth of the rate-limiting substrate is uniform throughout the reactor, so the overall rate of substrate degradation in the reactor can be evaluated by Eq. (3).

$$r = k_{of} A L_{pen} \quad (3)$$

where r is the overall rate of substrate degradation in the reactor and A is the total active surface area for bacterial growth. The combination of Eqs. (1) and (3) gives Eq. (4).

$$r = A \sqrt{2S^b D_f k_{of}} \quad (4)$$

Following assumptions (5) and (6), the volumetric gas-liquid transfer rate through the gas-liquid interface can be described by Eq. (5) [12].

$$dC/dt = k_L \alpha (C^* - C) \quad (5)$$

where C is the concentration in liquid; C\* is the equilibrium concentration in the liquid according to Henry's law and k<sub>L</sub>a is the overall volumetric gas-liquid mass transfer coefficient. In the k<sub>L</sub>a expression, k<sub>L</sub> equals to (D/δ) and a equals to (A/V), where D is the diffusivity in the interfacial liquid film; δ is the width of the interfacial liquid film; A is the interfacial surface area and V is the representative volume, usually taken as the liquid volume or the overall volume of the system. The k<sub>L</sub>a is highly affected by temperature, flow conditions and the interfacial gas-liquid surface area, and can be calculated mechanistically [13] or estimated empirically from mass balance equations [14]. In the UFPR, k<sub>L</sub>a can be evaluated empirically by analytical solution of the mass balance equations as will be shown later.

Eqs. (6) and (7) describe the general mass balances in the reactor for NO<sub>3</sub><sup>-</sup>-N and dissolved H<sub>2</sub>, respectively.

$$V(dN_e/dt) = Q(N_i - N_e) - r_N V \quad (6)$$

$$V(dH_e/dt) = k_L \alpha (H^* - H_{av}) V + Q(H_i - H_e) - r_H V \quad (7)$$

where V is the reactor volume; N<sub>e</sub> and H<sub>e</sub> are the concentration of NO<sub>3</sub><sup>-</sup>-N and dissolved H<sub>2</sub> in the effluent, respectively; k<sub>L</sub>a is the overall volumetric gas-liquid mass transfer coefficient of H<sub>2</sub>; H<sub>av</sub> is the average concentration of dissolved H<sub>2</sub> along the filter; t is the time

component; Q is the volumetric flow rate; N<sub>i</sub> and H<sub>i</sub> are the concentration of NO<sub>3</sub><sup>-</sup>-N and dissolved H<sub>2</sub> in the influent, respectively; H\* is the equilibrium concentration of dissolved H<sub>2</sub> and r<sub>N</sub> and r<sub>H</sub> are the overall degradation rates of NO<sub>3</sub><sup>-</sup>-N and dissolved H<sub>2</sub>, respectively.

Following assumption (1) above and assuming that the concentration of dissolved H<sub>2</sub> in the influent is close to zero (H<sub>i</sub> ≈ 0), at steady-state conditions Eqs. (6) and (7) can be simplified to form Eqs. (8) and (9), respectively.

$$0 = Q(N_i - N_e) - r_N V \quad (8)$$

$$0 = k_L \alpha (H^* - H_{av}) V - QH_e - r_H V \quad (9)$$

H\* is calculated according to Henry's law by Eq. (10).

$$H^* = P_{H_2} C_{H_2} \quad (10)$$

where C<sub>H<sub>2</sub></sub> is Henry's constant for H<sub>2</sub> in units of mg/(L·bar) and P<sub>H<sub>2</sub></sub> is the partial pressure of H<sub>2</sub> gas in the reactor calculated by Eq. (11) according to the concept developed [2].

$$P_{H_2} = P_T - P_{N_2} \quad (11)$$

where P<sub>T</sub> is the total pressure (i.e., pressure of H<sub>2</sub> and N<sub>2</sub> gases) in the reactor and P<sub>N<sub>2</sub></sub> is the partial pressure of N<sub>2</sub> gas in the reactor calculated by Eq. (12) according to Henry's law.

$$P_{N_2} = N_{2,T} / C_{N_2} \quad (12)$$

where C<sub>N<sub>2</sub></sub> is Henry's constant for N<sub>2</sub> in units of mg/(L·bar) and N<sub>2,T</sub> is the total dissolved N<sub>2</sub> concentration calculated by Eq. (13).

$$N_{2,T} = N_{2,atm} + N_{2,denit} \quad (13)$$

where N<sub>2,atm</sub> is the dissolved N<sub>2</sub> concentration originated from atmospheric N<sub>2</sub> gas (assumed to be constant at stable outdoor temperature) and N<sub>2,denit</sub> is the dissolved N<sub>2</sub> concentration originated from denitrification and calculated by Eq. (14).

$$N_{2,denit} = 0.96 (N_i - N_e) \quad (14)$$

where 0.96 is the fraction of NO<sub>3</sub><sup>-</sup>-N converted to N<sub>2</sub> (catabolism) according to the hydrogenotrophic denitrification metabolic stoichiometry equation suggest by McCarty [15].

Eqs. (15) and (16) describe r<sub>N</sub> and r<sub>H</sub> in Eqs. (8) and (9) for conditions of NO<sub>3</sub><sup>-</sup>-N and H<sub>2</sub> limitation, respectively, according to Eq. (4).

$$\text{NO}_3^- - \text{N limitation} : r_N = A \sqrt{2D_{f,N} k_{of,N} N_{av}}; \quad r_H = \nu r_N \quad (15)$$

$$\text{H}_2 \text{ limitation} : r_N = \left(\frac{1}{\nu}\right) r_H; \quad r_H = A \sqrt{2D_{f,H} k_{of,H} H_{av}} \quad (16)$$

where the terms A√(2D<sub>f,N</sub>k<sub>of,N</sub>) and A√(2D<sub>f,H</sub>k<sub>of,H</sub>), the half-order coefficients for NO<sub>3</sub><sup>-</sup>-N and H<sub>2</sub>, respectively, will be referred to as K<sub>N</sub> and K<sub>H</sub>, respectively; D<sub>f,N</sub> and D<sub>f,H</sub> are the diffusivities of NO<sub>3</sub><sup>-</sup> and H<sub>2</sub> in the biofilm, respectively; k<sub>of,N</sub> and k<sub>of,H</sub> are the intrinsic maximal degradation rates (q<sub>max</sub>X<sub>f</sub>) of NO<sub>3</sub><sup>-</sup>-N and H<sub>2</sub> in the biofilm, respectively; A is the total active surface area for bacterial growth; ν is the stoichiometric mass ratio {H<sub>2</sub>:NO<sub>3</sub><sup>-</sup>-N}; and N<sub>av</sub> and H<sub>av</sub> are the average bulk concentrations of NO<sub>3</sub><sup>-</sup>-N and dissolved H<sub>2</sub> along the filter, respectively, calculated as a simple mean of the concentration in the upper part of the column (i.e. merge of recirculation flow and inflow) and in the effluent (Eq. (17a) and (17b)).

$$N_{av} = \frac{N_i Q + N_e Q_R + N_e}{Q + Q_R}; \quad (17a)$$

$$H_{av} = \frac{H_i Q + H_e Q_R + H_e}{Q + Q_R} \quad (17b)$$

where Q<sub>R</sub> is the recirculation flow rate.

Interestingly, preliminary observations showed that the half-order coefficients  $K_N$  and  $K_H$  vary with different average bulk concentration of the rate-limiting substrate (i.e.  $N_{av}$  or  $H_{av}$ , respectively). Therefore, new terms  $\beta_N$  and  $\beta_H$  were incorporated to correct  $K_N$  and  $K_H$ , respectively, for a specific average bulk concentration of the rate-limiting substrate. The correction factors  $\beta_N$  and  $\beta_H$  are required in order to take into account the influence of pH increase in the biofilm on  $q_{max}$ , deviation from zero-order degradation kinetics within the biofilm due to low substrate concentrations and non-homogeneity of the biofilm. These three mechanisms are assumed to depend on the average bulk concentration of the rate-limiting substrate, as discussed in Section 4.2.

Following the above consideration, the terms  $r_N$  and  $r_H$  in Eqs. (15) and (16) can be modified to form Eqs. (15') and (16'), respectively.

$$\text{NO}_3^- - \text{N limitation} : r'_N = \beta_N A \sqrt{2D_{f,N} k_{of,N} N_{av}}; r'_H = \nu r_N \quad (15')$$

$$\text{H}_2 \text{ limitation} : r'_N = \left(\frac{1}{\nu}\right) r_H; r'_H = \beta_H A \sqrt{2D_{f,H} k_{of,H} H_{av}} \quad (16')$$

where  $\beta_N$  and  $\beta_H$  are the correction factors for the half-order coefficients  $K_N$  and  $K_H$ , respectively, and defined by Eq. (18a) and (18b).

$$\beta_N = f_1(N_{av}); \quad (18a)$$

$$\beta_H = f_2(H_{av}) \quad (18b)$$

where  $f_1$  and  $f_2$  are functions describing  $\beta_N$  and  $\beta_H$ , respectively.

$k_L a$  in Eq. (9) and  $A$  in Eqs. (15) and (16) are assumed to depend on the total flow rate over the media, i.e. the sum of recirculation flow rate and the volumetric flow rate (Eqs. (19) and (20)).

$$k_L a = f_3(Q_R + Q) \quad (19)$$

$$A = f_4(Q_R + Q) \quad (20)$$

where  $f_3$  and  $f_4$  are functions describing  $k_L a$  and  $A$ , respectively.

A detailed list summarizing the main model variables is shown in Table 1.

In Table 1, input variables are defined as independent variables controlled directly by the operator or dictated by the local constraints. Intermediate variables are defined as variables that depend uniquely on specific input variables and are not controlled directly by the operator. Output variables depend on a complex ensemble of all input and intermediate variables. The empirical correction factors  $\beta_N$  and  $\beta_H$  are exceptional intermediate variables, depending on a preliminary assessment of the average bulk sub-

strate concentration of the rate-limiting substrate (i.e.  $N_{av}$  or  $H_{av}$ ). Other important parameters can be derived from the output variables such as denitrification rate and  $\text{H}_2$  utilization efficiency.

Since input variables are given, model solution (i.e. calculation of all output variables) can be accomplished after finding the functions describing the intermediate variables (see Eqs. (18a), (18b), (19) and (20)), which link the input and the output variables. Therefore, evaluation of the intermediate variables for different sets of conditions is the main stage in model development. Detailed explanations and test protocols of methods to assess the intermediate variables are given in the next section.

### 3. Materials and methods

#### 3.1. Experimental setup

The unsaturated-flow pressurized reactor (UFPR) used for all continuous tests is shown in Fig. 1. A detailed description of the system and reactor start-up was given in an earlier publication [2]. Briefly, it comprised of a clear PVC cylindrical reactor 71 cm in height and 10.5 cm in diameter divided into two unequal parts. The top part of the reactor (height 51 cm) contained plastic biofilm carriers (total surface of  $900 \text{ m}^2/\text{m}^3$ , Aqwise) and was separated by a metal screen from the bottom part (height 20 cm) of the reactor where recirculating water collected. The reactor was connected to a gas supply ( $\text{H}_2$  cylinder with pressure regulator), feed pump (Diaphragm pump model 7090-42, Cole-Palmer), recirculation pump (FL-2403, ProPumps) and pH controlling unit (standard pH electrode, pH controller – pH190, Alpha; hydrochloric acid tank and acid pump – gamma/L, ProMinent).

The feed solution for all experiments was tap water mixed with concentrated stock solutions of  $\text{NaNO}_3$  and  $\text{KH}_2\text{PO}_4$ . The specific operational conditions used for each test are elaborated in the test protocols section. Water temperature was maintained constant at  $27.5 \pm 1 \text{ }^\circ\text{C}$ . Bulk pH was kept at  $7 \pm 0.1$  by dosing hydrochloric acid. The relatively low pH was aimed to prevent an extreme pH increase within the biofilm, which leads to  $\text{NO}_2^-$ -N accumulation [7,16]. Influent and effluent water were collected for further analyses.

For all continuous experiments, the system was first operated to steady state with the highest  $Q_R$  (i.e. 8000 mL/min), high average  $\text{NO}_3^-$ -N concentration above 20 mg/L (i.e.  $N_{av} > 20 \text{ mg/L}$ ) and high  $\text{H}_2$  pressure of 3 bars, achieved by continuous gas flushing of the reactor's headspace with  $\text{H}_2$  gas under pressure of 3 bars. The volumetric flow rate was 450 mL/min and  $N_{av}$  was controlled by adjusting the inlet  $\text{NO}_3^-$ -N concentration (i.e.  $N_i$ ). For the current research purposes, steady state was defined as an operational state presenting constant denitrification rate during extended operation.

**Table 1**  
Detailed list of the main model variables.

Variable	Symbol	Type of variable	Dependency
Volumetric flow rate	$Q$	Input	Operator
$\text{NO}_3^-$ -N inlet concentration	$N_i$	Input	Local constraints
Total pressure	$P_T$	Input	Operator
Reactor volume	$V$	Input	Operator
Recirculation flow rate	$Q_R$	Input	Operator
Total flow rate	$Q_R + Q$	Input	Operator
Overall volumetric gas ( $\text{H}_2$ )-liquid mass transfer coefficient	$k_L a$	Intermediate	$Q_R$ and $Q$
Half-order coefficient	$K_N, K_H$	Intermediate	$Q_R$ and $Q$
Empirical correction factors for $K_N$ and $K_H$	$\beta_N, \beta_H$	Intermediate	See explanation in body text below
$\text{NO}_3^-$ -N effluent concentration	$N_e$	Output	Input and intermediate variables
Dissolved $\text{H}_2$ effluent concentration	$H_e$	Output	Input and intermediate variables
Equilibrium concentration of dissolved $\text{H}_2$	$H^*$	Output	Input and intermediate variables
Partial pressure of $\text{H}_2$	$P_{\text{H}_2}$	Output	Input and intermediate variables
Partial pressure of $\text{N}_2$	$P_{\text{N}_2}$	Output	Input and intermediate variables

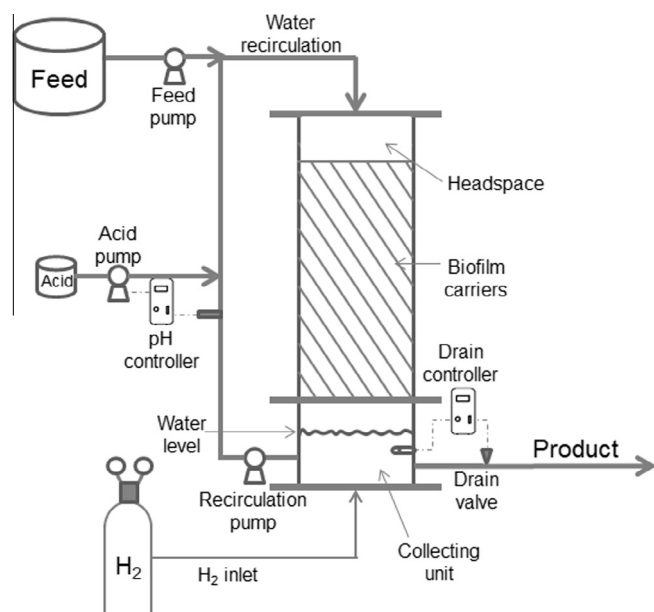


Fig. 1. Schematic diagram of the UFPR system.

All test protocols described in Section 3.4 were conducted after reaching steady state.

### 3.2. Preliminary batch experiment to determine the maximal specific degradation rate of $\text{NO}_3^-$ -N

The intrinsic maximal specific degradation rate of  $\text{NO}_3^-$ -N,  $q_{\max,N}$ , was found in a separate batch experiment with suspended growth medium at similar conditions as in the bulk liquid in the biofilm experiments (i.e. pH 7 and temperature of 27.5 °C). A 4.5 L mixed liquor volatile suspended solid (MLVSS) solution with biomass taken from the biofilm reactor was mixed with 2 L of tap water together with 3.7 g  $\text{NaNO}_3$ , 6 g  $\text{NaHCO}_3$  and 0.3 g  $\text{KH}_2\text{PO}_4$ . A constant  $\text{H}_2$  pressure of 2 bars was maintained during the experiment by continuous  $\text{H}_2$  sparging. Nitrate-N concentration was measured over time and denitrification rate was calculated. Following measurement of the volatile suspended solids (VSS) concentration,  $q_{\max,N}$  was calculated using the Lineweaver-Burk plot method. The VSS concentration was measured according to Standard Methods (Method 2540).

### 3.3. Analytical methods

Nitrate was determined using a Metrohm 761 ion chromatograph (IC) equipped with a 150 mm Metrosep A Supp 5 column with column guard and suppressor using a  $\text{CO}_3^{2-}/\text{HCO}_3^-$  eluent. Nitrite-N and alkalinity were measured according to Standard Methods (Method 4500 and Method 2320, respectively).

Biofilm density  $X_f$  was measured by the following procedure: (1) biofilm originating from the experimental system was separated from the plastic carriers in tap water to create MLVSS solution; (2) a 25 mL of the MLVSS solution was allowed to settle in a 50 mL measuring cup; (3) after settling, the volumes of clear water phase and settled biomass phase were recorded; (4) the total volume was filtered and the biomass volume was calculated by subtracting the filtered water volume from the total tested volume (i.e. 25 mL); (5) VSS weight was measured; (6) biofilm density was calculated by dividing the VSS weight by the biomass volume.

## 3.4. Test protocols for assessment of model's intermediate variables

### 3.4.1. Assessment of the half-order coefficients $K_N$ and $K_H$ for different recirculation flow rates

In this experiment,  $\text{H}_2$  was given in excess by continuous flushing of the reactor's headspace with  $\text{H}_2$  gas under pressure of 3 bars. The average  $\text{NO}_3^-$ -N concentration  $N_{av}$  was kept constant at 5 mg/L by adjusting the inlet  $\text{NO}_3^-$ -N concentration  $N_i$  in the range of 20–40 mg/L. With  $\text{NO}_3^-$ -N as the rate limiting substrate, Eq. (15) could be used and  $K_N$  and  $K_H$  were assessed for different  $Q_R$  values in the range of 1250–8000 mL/min. For each recirculation flow rate applied,  $N_i$  and  $N_e$  were measured, the denitrification rate  $r_N$  was calculated by Eq. (8) and  $K_N$  was calculated by Eq. (15). Finally, a mathematical expression for  $K_N$  as a function of the total flow rate (i.e.  $Q_R + Q$ ) at  $N_{av} = 5$  mg/L was derived in MS Excel and the corresponding expression for  $K_H$  was also determined as explained in Section 4.1.

### 3.4.2. Assessment of the correction factors $\beta_N$ and $\beta_H$ for $K_N$ and $K_H$

For assessing  $\beta_N$  and  $\beta_H$ ,  $\text{H}_2$  was given in excess as described in Section 3.4.1. The recirculation flow rate  $Q_R$  was kept constant on 8000 mL/min and  $\beta_N$  and  $\beta_H$  were assessed for different  $N_{av}$  concentrations in the range of 0–20 mg/L by adjusting the  $N_i$  in the range of 10–75 mg/L. For each value of  $N_{av}$  tested,  $N_i$  and  $N_e$  were measured, the denitrification rate  $r_N$  was calculated by Eq. (8), the product  $K_N\beta_N$  was calculated by Eq. (15') and divided by the reference  $K_N$  calculated in Section 3.4.1 (i.e.  $K_N$  at  $N_{av} = 5$  mg/L and  $Q = 8000$  mL/min) to find  $\beta_N$  for the specific  $N_{av}$  value. Finally, a mathematical expression for  $\beta_N$  as a function of  $N_{av}$  was derived in MS Excel and the corresponding expression for  $\beta_H$  was also determined as explained in Section 4.2.

### 3.4.3. Assessment of the overall volumetric gas ( $\text{H}_2$ )-liquid mass transfer coefficient $k_La$ for different recirculation flow rates

For assessing  $k_La$  values by Eq. (9),  $H_{av}$  values are initially had to be calculated by Eq. (16'). In order to use Eq. (16'),  $\text{H}_2$  was set to be limiting by continuous flushing of the reactor's headspace with  $\text{H}_2$  gas under a lower pressure of 1.5 bars and keeping the  $N_{av}$  values above 36 mg/L by applying a constant  $N_i$  of 65 mg/L. The  $k_La$  values were assessed for different  $Q_R$  values in the range of 1250–8000 mL/min. For each  $Q_R$  applied, the following procedure was performed: (1)  $N_i$  and  $N_e$  were measured; (2) the denitrification rate  $r_N$  was calculated by Eq. (8) and converted to  $\text{H}_2$  degradation rate  $r_H$  by the stoichiometric mass ratio  $\nu$ ; (3) an initial assessment of  $H_{av}$  was done by Eq. (16) using the reference value of  $K_H$  calculated in Section 3.4.1; (4) the corresponding  $\beta_H$  for the initial  $H_{av}$  assessed was calculated by the expression derived in Section 3.4.2; (5) a corrected  $H_{av}$  value was calculated by Eq. (16') using the corresponding  $\beta_H$  found; (6) effluent  $\text{H}_2$  concentration (i.e.  $H_e$ ) was calculated by Eq. (17b); (7) the overall volumetric gas-liquid mass transfer coefficient  $k_La$  was calculated analytically by Eq. (9) using the corresponding  $H^*$  for  $\text{H}_2$  pressure of 1.5 bar according to Henry's law (i.e.  $H^* \approx 2.3$  mg/L). Following these 7 steps for all values of  $Q_R$  tested, a mathematical expression for  $k_La$  as a function of the total flow rate was derived in MS Excel.

## 3.5. Model utilization

Two important points should be noted regarding model utilization: (1) Since the correction factors  $\beta_N$  and  $\beta_H$  depend on the average concentration of the rate-limiting substrate (i.e.  $N_{av}$  or  $H_{av}$ , which are output variables and not known at the beginning), a calculation of a preliminary set of output variables using Eqs. (15) or (16) is performed. The preliminary  $N_{av}$  and  $H_{av}$  calculated are then served to assess the corresponding values of  $\beta_N$  and  $\beta_H$ , respectively, according to the procedure described in Section 3.4.2.

Afterwards, a new set of output variables is calculated with  $\beta_N$  and  $\beta_H$  found. Theoretically, this procedure should be repeated to increase the model's accuracy. However, a single iteration gave satisfactory results in most cases. (2) Since the choice between Eq. (15) or (16) depends on which substrate is limiting (determined only after knowing the output variables  $N_{av}$  and  $H_{av}$ ), both Eqs. (15) and (16) are initially used and the results are compared. The choice of the right equation to be carried forward during model use is tested in terms of substrate limitation by Eq. (21).

$$H_{av}/N_{av} = v \times (D_{f,N}/D_{f,H}) = 0.129 \text{ gH}_2/\text{gNO}_3^- \text{N} \quad (21)$$

Eq. (21) is a derivative of the equalization of Eq. (1) for  $N_{av}$  and  $H_{av}$ . The following values were taken for calculations:  $v = 0.429 \text{ g H}_2/\text{g NO}_3^- \text{N}$  [15],  $D_{f,N} = 8.15 \times 10^{-10} \text{ m}^2/\text{sec}$  and  $D_{f,H} = 2.7 \times 10^{-9} \text{ m}^2/\text{sec}$  [17].

## 4. Results and discussion

### 4.1. Assessment of the half-order coefficients $K_N$ and $K_H$ for different recirculation flow rates

The first set of continuous experiments (see Section 3.4.1) with  $\text{NO}_3^- \text{N}$  as the rate limiting substrate was performed in order to assess  $K_N$  values ( $K_N = A\sqrt{2D_{f,N}k_{of,N}}$ ) at constant  $N_{av}$  concentration of  $5 \text{ mg NO}_3^- \text{N/L}$  for different recirculation flow rates ( $Q_R$ ) by Eq. (15). The results for  $K_N$  at  $N_{av} = 5$  as a function of the total flow rate are shown in Fig. 2.

As expected,  $K_N$  values (with the corresponding denitrification rates) increased significantly with higher recirculation flow rates due to the increase in media wetting which results in higher surface area of active biofilm (i.e.  $A$  in the expression of  $K_N$  above) exposed to both  $\text{NO}_3^- \text{N}$  and  $\text{H}_2$  as discussed previously [2]. As mentioned above, the relatively high recirculation flow rate required to achieve full media wetting is mainly due to the high specific surface area of the carriers. High hydraulic loading rates were specifically reported for nitrifying trickling filters in recirculating aquaculture [3]. At  $Q_R + Q \approx 8000 \text{ mL/min}$ , media wetting approached a maximal level. Further increase of  $Q_R$  was not possible due to technical issues. A trend line with R-squared coefficient value of 0.9995 was determined (Eq. (22)).

$$K_N = -3 \times 10^{-5} (Q_R + Q)^2 + 0.487(Q_R + Q) + 11.5 \quad (22)$$

The corresponding  $H_{av}$  concentration with the same penetration depth as  $5 \text{ mg NO}_3^- \text{N/L}$  was estimated by Eq. (21) to be  $0.65 \text{ mg/L}$ . A mathematical expression for  $K_H$  as a function of the total flow rate at  $H_{av} = 0.65 \text{ mg/L}$  was derived by Eq. (23) and presented in Eq. (24).

$$K_H = K_N \sqrt{v \times (D_{f,H}/D_{f,N})} \quad (23)$$

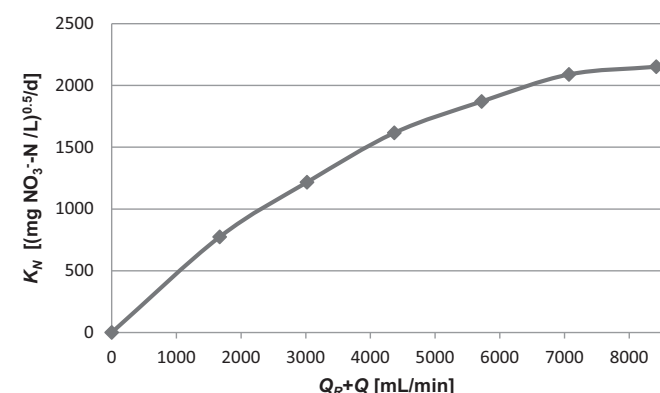


Fig. 2.  $K_N$  values at  $N_{av} = 5 \text{ mg NO}_3^- \text{N/L}$  as a function of the total flow rate  $Q_R + Q$ .

$$K_H = -3 \times 10^{-5} (Q_R + Q)^2 + 0.580(Q_R + Q) + 13.6 \quad (24)$$

### 4.2. Assessment of the correction factors $\beta_N$ and $\beta_H$ for $K_N$ and $K_H$

As was already mentioned in Section 2,  $K_N$  and  $K_H$  were found to vary slightly with different values of the average bulk concentration of the rate-limiting substrate (i.e.  $N_{av}$  or  $H_{av}$ ). The assumption here is that the concentration of the rate-limiting substrate governs the following mechanisms: (1) deviation from intrinsic zero-order kinetic: at higher concentration of the rate-limiting substrate, higher fraction of the penetration depth is dominated by intrinsic zero-order kinetic and  $K_N$  and  $K_H$  are increased; (2) effect of pH changes on  $q_{max}$ : at higher concentration of the rate-limiting substrate, higher penetration is achieved with the resulting formation of sub-biofilm layers working at higher pH gradient along the penetration depth. The gradual increase in pH along the penetration depth results in an increase in the maximal specific degradation rate  $q_{max}$  in the range of pH applied (i.e., ~7–9.5) [7], and therefore an increase in  $K_N$  and  $K_H$ ; (3) homogeneity of the biofilm: since the biofilm layer is not truly homogeneous, at higher concentrations of the rate-limiting substrate more regions in the reactor experience full substrate penetration and further increases in concentration should not lead to an increase in denitrification rate as predicted by the standard overall rate expression based on half-order kinetics (i.e. Eqs. (15) and (16)). This should reduce  $K_N$  and  $K_H$  with the increase in concentration.

In general, the effect of mechanisms (1) and (2) requires positive correction, while the effect of mechanism (3) requires negative correction for  $K_N$  and  $K_H$ . The empirical correction factors  $\beta_N$  and  $\beta_H$  in Eqs. (15') and (16') reflect the overall correction required to compensate for the effect of these 3 mechanisms on  $K_N$  and  $K_H$ , respectively.

Following the assumption above, a second set of experiments with  $\text{NO}_3^- \text{N}$  as the rate limiting factor was performed in order to assess the effect of different  $N_{av}$  concentrations on  $\beta_N$  values at constant total flow rate of  $8450 \text{ mL/min}$ . The results for  $\beta_N$  as a function of  $N_{av}$  are shown in Fig. 3.

Fig. 3 shows the overall effects of the three mechanisms mentioned above on  $\beta_N$  as a function of  $N_{av}$ . In general,  $\beta_N$  increased with higher  $N_{av}$  values for  $N_{av} < 12 \text{ mg/L}$ . For  $N_{av} < 5 \text{ mg/L}$  (i.e. below the reference concentration where  $\beta_N$  was set to be 1) it is assumed that mechanism 1 (i.e. deviation from zero-order kinetic) dominated the overall effects of the three mechanisms. For  $N_{av}$  in the range of 5–12 mg/L, the increase of  $\beta_N$  with higher  $N_{av}$  values may be related to the effect of mechanism 2 (i.e. pH changes). For  $N_{av} > 12 \text{ mg/L}$  mechanism 3 dominated the overall effects of the three mechanisms and  $\beta_N$  decreased with increased  $N_{av}$  values.

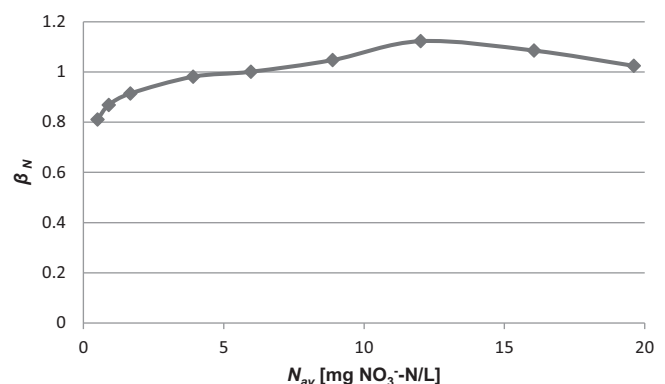


Fig. 3. The correction factor  $\beta_N$  for  $K_N$  as a function of different  $N_{av}$  concentrations at constant total flow rate ( $Q_R + Q$ ) of  $8450 \text{ mL/min}$ .

A trend line for  $\beta_N$  with R-squared coefficient value of 0.9571 was derived from Fig. 3 (Eq. (25)).

$$\beta_N = -0.0017 N_{av}^2 + 0.043 N_{av} + 0.820 \quad (25)$$

A trend line for  $\beta_H$  (Eq. (26)) was derived by combining Eq. (25) and (21).

$$\beta_H = -0.0993 H_{av}^2 + 0.334 H_{av} + 0.821 \quad (26)$$

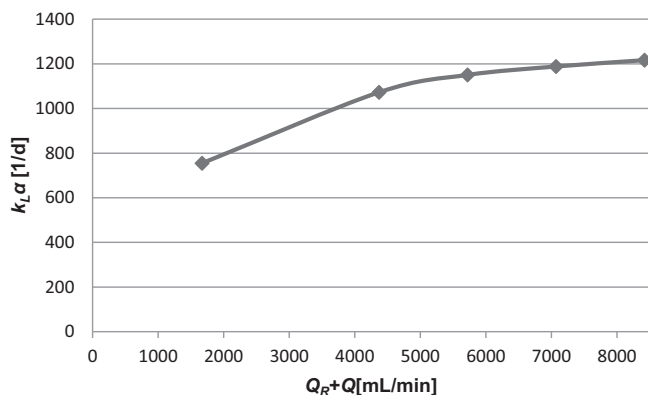


Fig. 4. The overall volumetric gas ( $H_2$ )-liquid mass transfer coefficient  $k_L a$  as a function of the total flow rate  $Q_R + Q$ .

#### 4.3. Assessment of $k_L a$ for different recirculation flow rates

Following the assessment of  $K_N$ ,  $K_H$ ,  $\beta_N$  and  $\beta_H$ , a third set of experiments was conducted in order to assess the overall volumetric gas ( $H_2$ )-liquid mass transfer coefficient  $k_L a$  for different total flow rates. In this case,  $NO_3^- - N$  was given in excess to ensure limitation of  $H_2$ . The results are shown in Fig. 4.

Fig. 4 shows that  $k_L a$  values increased with higher recirculation flow rates. The main reason is the increase in media wetting for higher values of  $Q_R$  and therefore an increase in the gas-liquid interfacial surface area ( $k_L a = k_L \times A/v$ ). Media wetting has been reported to be a prominent parameter affecting  $k_L a$  in biotrickling filters for volatile organic compounds (VOCs) [18] and waste gases removal [19]. In both reports,  $k_L a$  values for  $O_2$  gas-liquid transfer in the range of 500–2500 1/d were reported. Estrada et al. also linked water recirculation intensity (expressed as liquid velocity) to  $k_L a$  [20]. Reports on  $k_L a$  values for other hydrogenotrophic denitrification systems were not found. A trend line for  $k_L a$  with R-squared coefficient value of 0.9975 was derived (Eq. (27)).

$$k_L a = -10^{-5} (Q_R + Q)^2 + 0.181 (Q_R + Q) + 487 \quad (27)$$

The  $k_L a$  value was not evaluated at lower recirculation flow rates which are not relevant for the operational conditions of the UFPR.

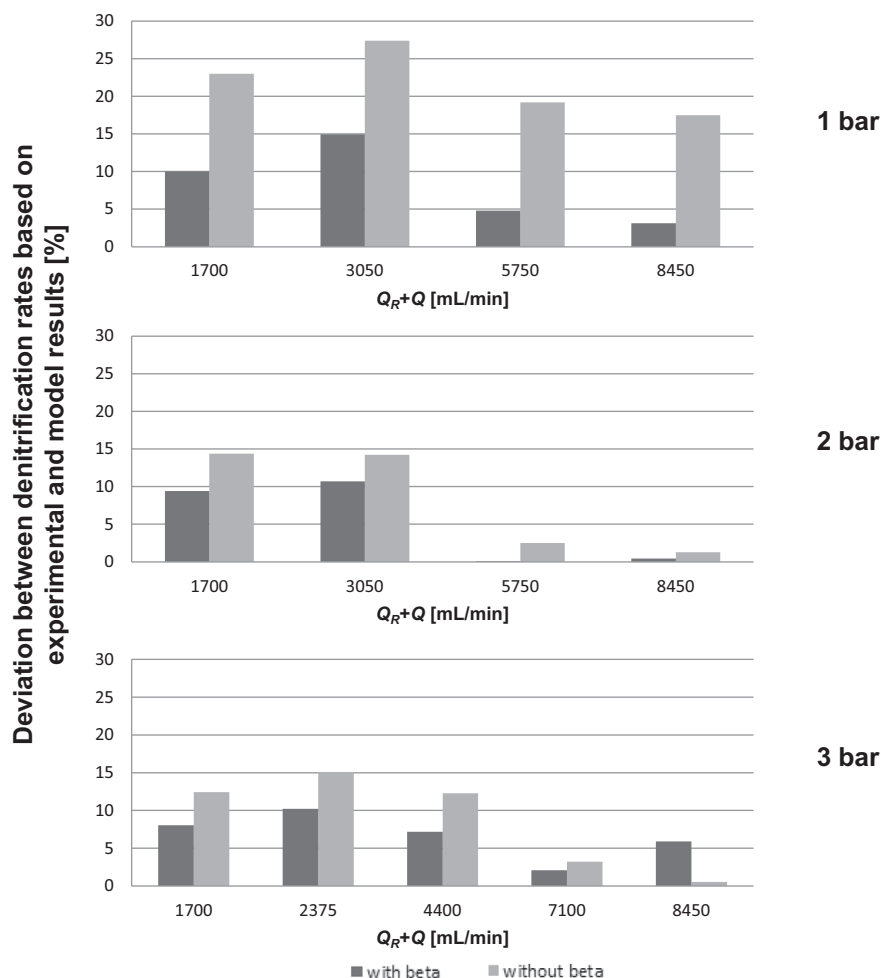


Fig. 5. Deviation between denitrification rates based on experimental and model results (Y axis) for different combinations of recirculation flow rate (X axis) and  $H_2$  pressure – with and without the correction factor  $\beta$  (see legend).

#### 4.4. Model validation

Following the evaluation of the intermediate variables (i.e.  $k_L a$ ,  $K_N$ ,  $K_H$ ,  $\beta_N$  and  $\beta_H$ ), a set of experiments was conducted in order to validate the model. Denitrification rates measured for various combinations of recirculation flow rates ( $Q_R$ ) and  $H_2$  pressures were compared to those calculated by the model with and without the correction factor  $\beta$ . Normally, the UFPR is operated with closed headspace under a constant total pressure determined by the operator. During operation, the  $H_2$  partial pressure decreases and is replaced by  $N_2$  partial pressure (formed by denitrification) till a steady state is achieved with constant partial pressures of both

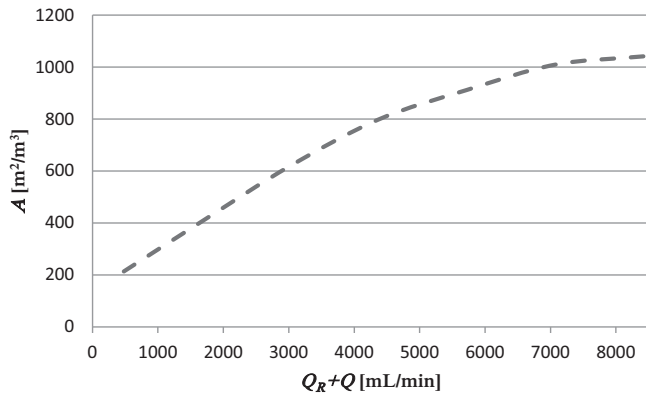


Fig. 6. Estimated active surface area  $A$  as a function of the overall loading rate  $Q_R + Q$ .

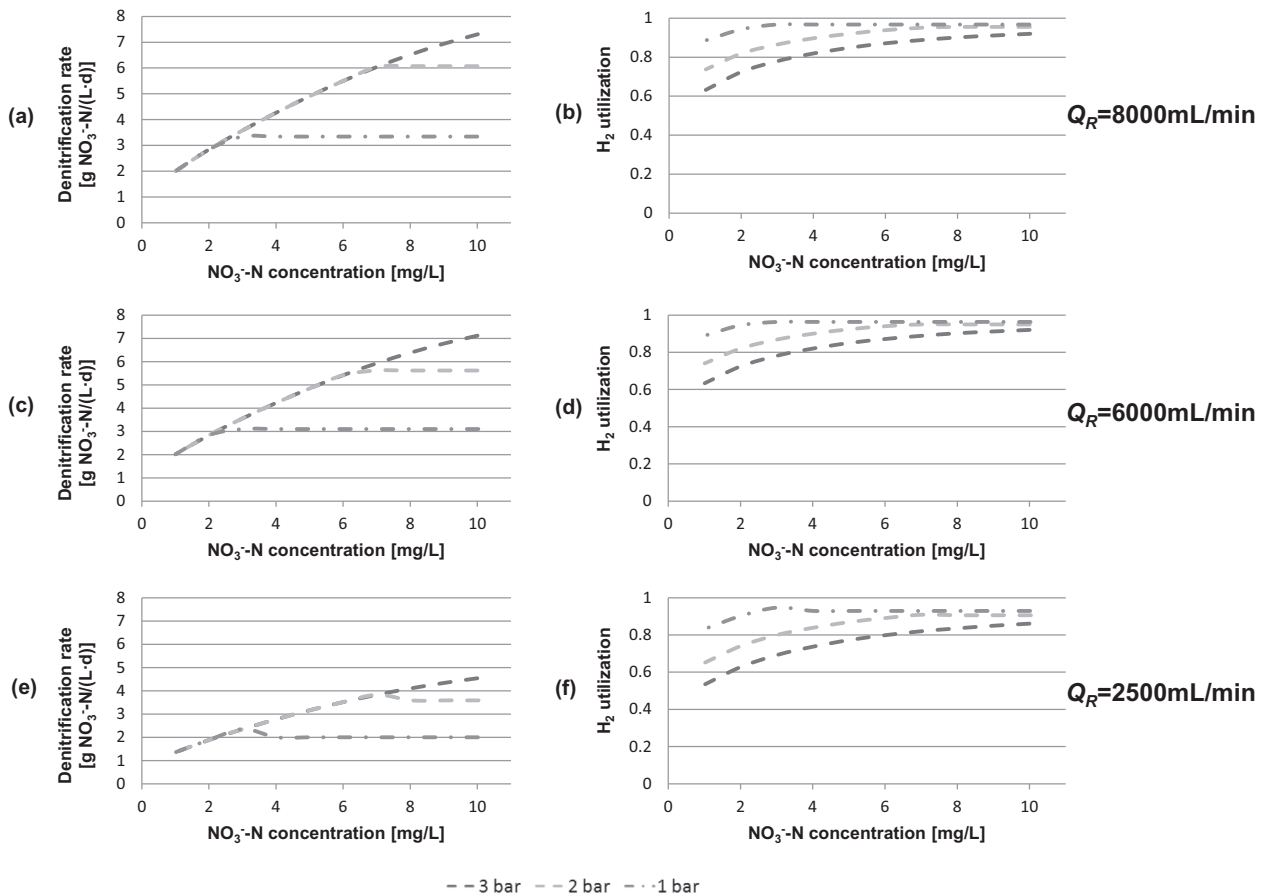


Fig. 7. Denitrification rate (a,c,e) and  $H_2$  utilization efficiency (b,d,f) predicted by the model as a function of effluent  $NO_3^-$ -N concentration for  $Q_R$  of 8000 mL/min (a,b), 6000 mL/min (c,d) and 2500 mL/min (e,f), and for  $H_2$  pressure of 1, 2 and 3 bars (see legend below figures).

gases. Here, however, the  $H_2$  pressure in each of the experiments was maintained constant from the beginning by continuous flushing of the reactor's headspace with  $H_2$  gas to ensure steady state conditions under a stable and known  $H_2$  pressure within the reactor (the corresponding total pressure in normal operation will be higher than the  $H_2$  pressure applied here). The deviation between model and experimental results for each of the combination is shown in Fig. 5.

Fig. 5 shows clearly that the deviations between experimental and model results were lower with the correction factor  $\beta$  (except for the combination of  $Q_R = 8450$  mL/min and  $H_2$  pressure of 3 bars). By incorporating  $\beta$ , high correlation between experimental and model results was observed for all combinations of  $Q_R$  and  $H_2$  pressure with average deviations of 8.2%, 5.2% and 6.7% for the trials with  $H_2$  pressure of 1, 2 and 3 bars, respectively. These minor deviations corroborate the use of the model developed in the previous sections for further evaluation of the UFPR performance.

#### 4.5. Performance Evaluation of the UFPR using the model

##### 4.5.1. Evaluation of the active surface area $A$ for different recirculation flow rates

The intrinsic maximal specific degradation rate of  $NO_3^-$ -N  $q_{max,N}$  and biofilm density  $X_f$  were found to be 0.606 g  $NO_3^-$ -N/(gVSS·d) and 0.05 gVSS/mL, respectively, using the procedures described in Section 3. Following the estimation of  $q_{max,N}$  and  $X_f$ , the maximal degradation rate of  $NO_3^-$ -N within the biofilm  $k_{of,N}$  could be calculated by Eq. (2). Combining the calculated  $k_{of,N}$  value with  $K_N$  values calculated for the different total flow rates may be used for



estimation of the active surface area  $A$  for different total flow rates ( $K_N = A\sqrt{2D_{f,N}k_{of,N}}$ ) by assuming constant average biofilm density (alternation of recirculation flow rates was performed for short periods and could hardly affect the average biofilm density). The results for the active surface area  $A$  calculated as a function of the total flow rate are shown in Fig. 6.

Fig. 6 shows that at the highest overall recirculation flow rate (i.e.  $Q_R + Q = 8450$  mL/min),  $A$  is close to the value of the total surface area of the carriers provided by the manufacturer (i.e.  $900$  m<sup>2</sup>/m<sup>3</sup>). This fact correlates with the above assumption that a maximal media wetting is achieved at total flow rate of approximately  $8450$  mL/min. In general, it is possible that the maximal value for  $A$  estimated by the model is a bit higher than the one provided by the manufacturer due to biomass adherence to other surfaces within the reactor except for the carriers.

#### 4.5.2. Evaluation of denitrification rate and H<sub>2</sub> utilization efficiency for different combinations of operational parameters

Denitrification rates and H<sub>2</sub> utilization efficiencies were evaluated by the model for various operational conditions (i.e. effluent NO<sub>3</sub><sup>-</sup>-N concentration, H<sub>2</sub> pressure and recirculation flow rate). The H<sub>2</sub> utilization efficiency was calculated by dividing H<sub>2</sub> consumption rate by the sum of H<sub>2</sub> consumption rate and H<sub>2</sub> loss through the effluent (Eq. (28)).

$$H_2 \text{ utilization} = r_H V / (r_H V + H_e Q) \quad (28)$$

Fig. 7 presents model results for denitrification rate (a,c,e) and H<sub>2</sub> utilization efficiency (b,d,f) as a function of the effluent NO<sub>3</sub><sup>-</sup>-N ( $N_e$ ) for different combinations of  $Q_R$  and H<sub>2</sub> pressure ( $P_{H_2}$ ). Fig. 7 (a,c,e) shows that NO<sub>3</sub><sup>-</sup>-N limits denitrification rates at low NO<sub>3</sub><sup>-</sup>-N concentrations. At higher NO<sub>3</sub><sup>-</sup>-N concentrations, H<sub>2</sub> was found to be the rate-limiting substrate since no improvement in denitrification rate was observed with increasing the NO<sub>3</sub><sup>-</sup>-N concentration. In general, at higher H<sub>2</sub> pressure, higher denitrification rates can be achieved and the NO<sub>3</sub><sup>-</sup>-N concentration at which the transition to H<sub>2</sub> limitation occurs is also higher. The increase in recirculation flow rate  $Q_R$  has also a positive effect on denitrification rates as discussed in Section 4.1.

The H<sub>2</sub> utilization efficiency is positively affected by increasing  $Q_R$ , although only in a minor way (Fig. 7 (b,d,f)). The reason for this is the higher H<sub>2</sub> consumption rate in the biofilm due to better media wetting for higher  $Q_R$  [2]. Operation at higher NO<sub>3</sub><sup>-</sup>-N concentrations also improves H<sub>2</sub> utilization efficiency in the case of NO<sub>3</sub><sup>-</sup>-N limitation due to the higher demand for H<sub>2</sub> by the biofilm. Obviously, higher H<sub>2</sub> pressure has a negative effect on H<sub>2</sub> utilization efficiency. At higher H<sub>2</sub> pressure, a higher amount of unutilized H<sub>2</sub> gas is dissolved in the liquid phase and released with the effluent.

In general, higher denitrification rates together with higher utilization efficiencies of H<sub>2</sub> are achieved in the UFPR as compared to other hydrogenotrophic systems reviewed previously [2]. Fig. 7 shows that high denitrification rates of up to  $7.5$  g NO<sub>3</sub><sup>-</sup>-N/(L<sub>reactor</sub>·d) together with H<sub>2</sub> utilization efficiency above 90% can be attained by the UFPR for operation under the regulatory NO<sub>3</sub><sup>-</sup>-N concentrations of below  $10$  mg/L.

## 5. Conclusions

A mathematical model based on simple mass balances for steady-state and completely stirred hydraulic conditions was sug-

gested for evaluating the performance of the novel unsaturated-flow pressurized reactor (UFPR) for hydrogenotrophic denitrification of groundwater. Increasing the total flow rate (i.e. recirculation + feed) up to  $8450$  mL/min with the corresponding recirculation ratio ( $Q_R/Q$ ) of 18 had a positive influence on the active surface area available for biofilm growth and gas (H<sub>2</sub>)-liquid mass transfer by improving media wetting. A correction factor  $\beta$  for the rate constant reduced the deviation between experimental and model results, by compensating for pH changes within the biofilm, deviation from intrinsic zero-order degradation kinetics and non-homogeneity of the biofilm. The addition of the correction factor resulted in a maximal deviation between measured and modeled denitrification rates of approximately 8%. Model results showed that high denitrification rates of up to  $7.5$  g NO<sub>3</sub><sup>-</sup>-N/(L<sub>reactor</sub>·d) together with H<sub>2</sub> utilization efficiency above 90% can be achieved in the UFPR. The principles for process evaluation using the model were described, making the treatment scheme proposed here easily adjustable to various regulatory requirements and water characteristics.

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